Substantial reduction of Stone-Wales activation barrier in fullerene

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Stone-Wales (SW) transformation is a key mechanism responsible for the growth, transformation, and fusion in fullerenes, carbon nanotubes, and other carbon nanostructures. These topological defects also substantially alter the physical and chemical properties of the carbon nanostructures. However, this transformation is thermodynamically limited by very high activation energy (≈7 eV in fullerenes). Using first-principles density functional calculations, we show that the substitutional boron doping substantially reduces the SW activation barrier (from ≈7 to 2.54 eV). This reduction is the largest in magnitude among all the mechanisms of barrier reduction reported to date. Analysis of bonding charge density and phonon frequencies suggests that the bond weakening at and around the active SW site in B heterofullerenes is responsible for such a reduction. Therefore, the formation of the SW defect is promoted in such heterofullerenes and is expected to affect their proposed H2 storage properties. Such substitutional doping also can modify the SW activation barrier in carbon nanotubes and graphene nanostructures and can catalyze isomerization, fusion, and nanowelding processes.

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I. INTRODUCTION

Stone-Wales (SW) defects1 are important topological defects in sp2-bonded carbon materials, which play crucial roles in the growth, isomerism, and nanoscale plasticity of carbon nanostructures, fullerenes, and graphitic nanostructures.2–4 SW transformation involves an in-plane 90°-bond rotation with respect to the bond center. This leads to pentagon-heptagon defects (5-7-7-5 dislocation dipole) in carbon nanotubes and graphene5–7 and the interchange of a pair of pentagonal and hexagonal rings in fullerenes.8 Such structural transformation is believed to be the fundamental unit process for the coalescence of fullerenes9 and nanotubes,7 the formation of molecular junctions for nanoelectronic devices,8 and plastic deformation.3 Both chemically modified and unmodified SW defects induce local curvature to the otherwise planar graphitic materials,5–7 which may enhance the formation of nanotubes and fullerenes from planar carbon nanostructures.13 Also, the coalescence of fullerenes and nanotubes has been proposed to occur through a sequence of such structural transformations.6,7 SW defects also alter the electronic properties of carbon nanostructures, and thus, substantially modify chemical reactivity toward adsorbates (reactivity increases compared to the pristine counterpart)14–17 and transport properties.18,19 Also, similar SW defects are observed in boron nitride nanotubes and nanosheets5,20 and are found to have important implications in determining the physical and chemical properties.21

It is known that 94% of the C60 isomers can be derived by a sequence of SW bond rotations.22 Thus, SW transformation is believed to be the fundamental mechanism for fullerene isomerism or Ih-C60 formation, which is the global minimum on the complex potential energy surface.23,24 Interchange of a pair of pentagonal and hexagonal rings in Ih-C60 via a single SW transition leads to C2v symmetry, which does not obey the isolated-pentagon rule.23 This is the first isomer, and it is separated by ≈1.6-eV energy from the global Ih minimum.26–28 Therefore, C2v-C60 represents the first step toward fullerene isomerism or the last step of the annealing process before reaching the icosahedral global minimum.23 Although earlier, the pristine C2v isomer was not observed experimentally, recently, the chlorinated C2v isomer was stabilized experimentally via Krätschmer-Huffman synthesis29 and in the gas phase by subsequent dechlorination.30 However, the SW transition in fullerenes is thermodynamically limited due to a very large activation barrier (≈7 eV, Fig. 1).27,31,32 This energy barrier is reduced in the presence of an extra carbon or hydrogen atom.2,33 The extra carbon atom acts as an autocatalyst and reduces the activation energy by ≈2 eV when preferentially placed in the regions of paired pentagons. In contrast, the endohedral metal doping (K, Ca, and La) is relatively less effective for barrier-height reduction.27

Here, we report the effect of substitutional doping on an SW transition in C60 through first-principles density functional calculations. We find that the activation barrier is reduced substantially by substitutional boron doping at the active SW sites. The quantitative reduction (2.12 and 4.34 eV for single and double B doping, respectively) is much larger compared to the cases with an extra carbon or hydrogen atom.2,33 Boron-doped heterofullerenes (C60-Bx, x ≲6) have been synthesized successfully34 and are believed to be a promising candidate for hydrogen storage.35,36 It has been shown that H2 adsorption energy increases substantially for B heterofullerenes where the B centers act as adsorption centers. The present paper shows that the formation of SW defects is promoted in such B-doped heterofullerenes, which may alter the reversible storage properties as SW defects are known to be more reactive toward adsorbates. Also, the presence of such a substitutional dopant is expected to reduce the activation barrier and to promote SW transition in other carbon nanostructures, and thus, to catalyze isomerism, fusion, and nanowelding processes.

II. METHODOLOGY

Calculations were carried out using density functional theory (DFT) implemented in the Vienna ab initio
The activation energy necessary for SW transition ($T_0 \rightarrow C_{2v}$) via the climbing-image NEB method requires structural information of the initial and final structures within the concerned level of theory. Therefore, before we discuss the effect of B doping on the SW activation barrier, we begin our discussion with the geometric and electronic properties of $C_{60}$, $C_{50}B$, and $C_{58}B_2$ cages.

### A. $C_{60}$, $C_{50}B$, and $C_{58}B_2$: Structural and electronic properties

There are two types of bonds in $I_h-C_{60}$: [6,6] bonds (1.399 Å) at the junctions of two hexagons are smaller than [5,6] bonds (1.453 Å) at the junctions of a pentagon and a hexagon. The $C_{2v}$ structure is the first isomer, and in agreement with previous theoretical reports, the global minimum structure is found to be 1.57-eV higher in energy compared to the $I_h$ structure. The optimized $C_{60}$ geometries for both $I_h$ and $C_{2v}$ symmetries are shown in Fig. 1, and a 14-atom pyracyclene region containing the rotating $C_2$ dimer is shown in Fig. 2(a). Calculated $\pi_-$ and $\pi$-bond lengths are in excellent agreement with previous theoretical calculations and experimental measurements for $I_h$-$C_{60}$. The rotating bond in $C_{2v}$-$C_{60}$ is much smaller (1.359 Å), which is also in agreement with previous theoretical calculations. However, no experimental information is available on pristine $C_{2v}$-$C_{60}$. Chlorinated $C_{2v}$ structure ($C_{60}Cl_2$) shows a similar bond shortening of the rotating dimer (1.37 Å). Such bond shortening introduces a local strain for the $C_{2v}$ structure, and thus, a distribution of the bond length is observed in the pyracyclene region.

When one of the $C$ atoms in the rotating dimer is replaced by B, three bond lengths involving C and B are increased (two [5,6]-C-B = 1.549 Å and one [6,6]-C-B = 1.524 Å) for $I_h$-$C_{50}B$ [Fig. 2(b)]. This is responsible for the bond deformation in the pyracyclene region of $C_{50}B$ with distribution ranges from 1.442 to 1.482 Å. The trend of the structural changes in moving from $I_h$-$C_{50}B$ to $C_{2v}$-$C_{50}B$ remains the same as observed for pristine $C_{60}$. The structural properties of $C_{58}B_2$ show similar qualitative behavior. The pyracyclene region is comparatively more deformed due to the presence of one B-B (1.663 Å) bond and four C-B (1.551 Å) bonds [Fig. 2(c)]. Although, strictly speaking, both $I_h$ and $C_{2v}$ symmetries are broken due to B doping; for simplicity, we will retain the same nomenclature throughout the paper.

Next, we briefly discuss the electronic properties. Pure $C_{60}$ is found to be a closed-shell singlet, whereas, doped B...
introduces a hole (one/B doping) into the system. We note that, for C59B, spin-polarized calculation lowers the total energy by 80 meV with respect to the non-spin-polarized calculation and yields a doublet state. In contrast, the C58B2 is a singlet, whereas, the triplet state lies significantly higher in energy.

The calculated Kohn-Sham energy gap between the highest occupied molecular level (HOMO) and the lowest unoccupied molecular level (LUMO) is 1.63 eV for \( I_h\)-C60. Conventional density functional calculations usually underestimate the HOMO-LUMO gap obtained from the Kohn-Sham eigenvalues, which is much lower than the quasiparticle energy gap.\(^{46–48}\) For an \( N \) electron molecular system, the quasiparticle energy gap can be defined as the difference between the ionization potential (IP = \( E[N−1]−E[N] \)) and the electron affinity (EA = \( E[N]−E[N+1] \)). Here, \( E[N] \) is the DFT total energy of a neutral system of \( N \) electrons. Our DFT-PBE calculations predict the IP and EA to be 7.32 and 2.75 eV, respectively, in agreement with previous DFT calculations.\(^{49}\) These results, and thus, the quasiparticle gap (4.57 eV) also agree well with the self-consistent \( GW \) calculations (\( IP = 7.41 \) eV and \( EA = 2.51 \) eV)\(^{50}\) and experimental measurements [\( IP = 7.54 ± 0.04 \) eV (Ref. 47) and \( EA = 2.65 ± 0.05 \) eV (Ref. 48)]. B heterofullerenes have somewhat smaller IP and bigger EA compared with C60 (Table I). These suggest that the formation of both cations and anions is relatively easier for B heterofullerenes, which indicate their enhanced redox characteristics.

Due to icosahedral symmetry, the Kohn-Sham HOMO (\( H_u \)) and LUMO (\( T_u \)) are five- and threefold degenerate, respectively, for \( I_h\)-C60. These degeneracies are lifted (Fig. 3) due to the presence of (1) a topological defect introduced by the SW transition and (2) substitutional B doping. Both cause a reduction in the HOMO-LUMO gap (Table I). For pristine \( C_{2v}\)-C60, the degeneracy of both the HOMO and the LUMO is completely broken (Fig. 3), and the HOMO-LUMO gap is reduced by \( \sim 0.7 \) eV (Table I).

Substitutional B introduces a significant bond deformation in the pyracyclene region [Figs. 2(b) and 2(c)], and thus, the inherent structural symmetries are broken. This removes the degeneracies of HOMO and LUMO levels (Fig. 3) and reduces the Kohn-Sham HOMO-LUMO energy gap (Table I). With subsequent B doping, the structural deformation increases [Figs. 2(b) and 2(c)], and thus, the energy gap decreases (Table I). Similarly, the presence of the SW defect further lifts the degeneracy (Fig. 3), and the gap is lower in the corresponding \( C_{2v}\) structures compared to the \( I_h \) heterofullerenes (Table I).

### B. Activation barrier: Effect of substitutional B doping

Activation barriers for the SW transition in carbon nanotubes, graphitic nanostructures, and fullerenes are generally very high.\(^{28,30,31}\) Our calculated energy barrier for pristine C60 is found to be 6.88 eV (Table II), which is in agreement with previous reports obtained within a range of theories.\(^{2,27,28,32}\)

| TABLE II. Although the activation barrier is underestimated in the PBE functional compared to the hybrid Hyed-Scuseria-Ernzerhof screened hybrid functional (HSE06), they show a similar qualitative trend. \( \delta E_a \) = \( E_a(C_{60}) − E_a(X) \) is the reduction in the activation barrier compared to pristine C60. |
|-----------------|-----------------|-----------------|-----------------|-----------------|
|                 | Activation barrier (eV) | \( \delta E_a \) (eV) |
|                 | PBE              | HSE06            | PBE              | HSE06            |
| C_{60}          | 6.88             | 7.61             |                  |                  |
| C_{60}^{+}      | 6.40             | 7.05             | 0.48 (0.56)      |                  |
| C_{59}B         | 4.76             | 5.22             | 2.12 (2.39)      |                  |
| C_{58}B_{2}     | 2.54             | 2.80             | 4.34 (4.81)      |                  |

![FIG. 3. (Color online) Kohn-Sham orbital degeneracy for pristine and substitutional B-doped fullerenes (C_{59}B and C_{58}B_{2}) for both \( I_h \) and \( C_{2v} \) symmetries. The HOMO (LUMO) of the icosahedral C_{60}, \( H_u \) (\( T_u \)) is fivefold (threefold) degenerate. Bottom (top) of the vertical arrow represents HOMO (LUMO). The introduction of defects, both in terms of topological defect and substitutional B, breaks the orbital degeneracy, and thus, reducing the Kohn-Sham energy gap \( E_{\delta} \) (see Table I).]
FIG. 4. (Color online) The activation energy barrier for the SW transition ($I_h \rightarrow C_{2v}$) reduces substantially for the B heterofullerenes when B is doped in the active SW sites (rotating dimer). The reverse barrier is smaller by an amount $\Delta E$ (Table I), which is similar in magnitude for all cages.

Compared to carbon nanotubes or graphitic nanostructures, the activation barrier in a fullerene is considerably less due to the strain present in the fullerene structure. We find that the rotating $C_2$ unit in the transition state (TS) pops out by $\sim 0.21$ Å from the $C_{60}$ surface. A similar TS was predicted previously. The bond length of the rotating $C_2$ unit shrinks to 1.248 Å in the TS from the corresponding bond lengths in $I_h$ and $C_{2v}$ symmetries.

We find that the large SW activation barrier is reduced substantially due to B doping (Table II and Fig. 4) at the active SW site. The barrier is reduced by 2.12 eV when a single C atom is replaced in the rotating dimer by B in the $C_{59}B$ heterofullerene. The reduction is comparable in magnitude with the cases where an extra carbon is strategically placed in the regions of paired pentagons or is catalyzed by hydrogen. In contrast, the endohedral metal doping has a relatively smaller effect where the barrier is found to reduce by only 0.80 eV for La doping. As we discussed earlier, the fact that $C_{59}B$ develops a (doublet) spin moment, we recalculated the activation barrier including spin polarization. We find that the spin-polarized activation barrier (4.67 eV) is only slightly lower than the non-spin-polarized calculation (4.76 eV).

Similar to $C_{59}B$, the activation barrier becomes lower in the singly charged fullerene $C_{60}^+$ compared to the neutral $C_{60}$. Although $C_{59}B$ is isoelectronic with $C_{60}^+$, the quantitative reduction in the activation barrier is much higher for $C_{59}B$ (2.12 eV) compared to $C_{60}^+$ (0.48 eV). The doped B not only introduces a localized hole, but also introduces a substantial local strain. The active C-B bonds are much larger than the C-C bonds, and thus, the activation barrier is much lower for the case of B doping.

The activation barrier is further reduced to 2.54 eV (Table II and Fig. 4) when both C atoms in the rotating dimer are replaced with B atoms for the $C_{58}B_2$ heterofullerene. Compared to pristine $C_{60}$, a total reduction of 4.34 eV is obtained, which is the maximum reported to date.

We find that the structure corresponding to the saddle point for all cages has only one vibrational mode with an imaginary frequency. This confirms that the obtained saddle points are indeed true first-order transition states. Frequency of the imaginary mode decreases with subsequent B doping (962, 377, and 167 cm$^{-1}$ for $C_{60}$, $C_{59}B$, and $C_{58}B_2$, respectively). Thus, the variation in energy along the reaction path becomes slower, i.e., the NEB curve gets flatter, with the introduction of boron (Fig. 4).

To confirm the trend observed in the activation barrier, we have recalculated the same using an HSE06. Although the PBE functional underestimates the activation barrier, the qualitative trend is found to be the same with the HSE06 functional (Table II). HSE06 activation barriers are calculated using the PBE reaction path and performing a single-point calculation on each intermediate image.

The origin of reduction in the SW activation barrier can be explained in terms of changes in bond strength, charge density, and phonon spectra, which point toward bond

FIG. 5. (Color online) Bonding charge densities $\Delta \rho$ for pristine $C_{60}$, single, and double B-doped heterofullerenes. The B atoms are shown in green. The $\Delta \rho$ for a particular cage is calculated as $\Delta \rho = \rho^{C_{60}}(r) - \rho^{C_{59}B}(r) - \rho^{C_{58}B_2}(r)$, where $X-Y$ represents the rotating C-C, C-B, and B-B dimers for $C_{60}$, $C_{59}B$, and $C_{58}B_2$ structures, respectively. For pristine $C_{60}$, the charge accumulation centers (red) appear at the middle of the bond, which indicate covalent C-C bonds. In contrast, due to B doping, the charge accumulation centers significantly shift toward the C atoms (shown with the arrows) indicating the ionic C-B character.
weakening at and around the rotating dimer. First, we calculate C-C, C-B, and B-B bond strengths in pristine C60, C59B, and C58B2, respectively, which can be calculated approximately using the following expressions:

\[
E_{C-C} = \frac{E^{\text{tot}}_{C60}}{90},
E_{C-B} = \left[ E^{\text{tot}}_{C59B} - 87 \times E_{C-C} \right]/3,
E_{B-B} = \left[ E^{\text{tot}}_{C58B2} - 85 \times E_{C-C} - 4 \times E_{C-B} \right],
\]

where \(E^{\text{tot}}\) represents the total binding energy of the respective structure. We find that \(E_{C-C} (5.87 \text{ eV}) > E_{C-B} (4.74 \text{ eV}) > E_{B-B} (3.75 \text{ eV})\). Due to these weaker C-B bonds around the rotating dimer, the SW rotation becomes easier for the heterofullerenes. We further notice that the amount of reduction is related to the reduction in bond strength as \(\delta E_{b} = n \times [E_{C-C} - E_{C-B}]\), where \(n\) is the number of C-B bonds involved in the SW transition for C59B (two) and C58B2 (four) heterofullerenes.

Bonding charge-density analysis (Fig. 5) also qualitatively points toward softening of the bonds that are involved in the SW process. Figure 5 shows the bonding charge densities for pristine C60 and B-doped heterofullerenes. For C60, the C-C bonding is completely covalent i.e., the bonding charge accumulates at the centers of the bond. This picture deviates for B-doped cases, where the charge accumulation centers move toward the C atom for C-B bonds, imparting ionic character to the C-B bonds. Thus, the C-C rotation is increasingly easier for C59B and C58B2 heterofullerenes. Also, the bonding character can be understood quantitatively from Bader charge analysis,\(^{54}\) which reveals that each B atom loses an \(\sim 1|e|\) charge to the neighboring C atoms, which also indicate the deviation from perfect covalent character.

Next, we turn our attention to the phonon frequencies calculated at the \(\Gamma\) point. It is reasonable to assume that the atoms around the rotating dimer are mostly affected due to B doping and SW rotation. Thus, we considered the 14-atom pyracyclene ring around the rotating bond to calculate the normal vibrational modes. This significantly reduces the size of the Hessian matrix (from \(180 \times 180\) for the full cluster to \(42 \times 42\) for the pyracyclene ring) to calculate phonon frequencies. Due to B doping, phonon frequencies gradually shift to the lower frequencies (Fig. 6). This indicates that the bonds get softer as phonon frequency \(\nu\) is related to bond stiffness \(k\), \(\nu \propto \sqrt{k}\). The observed softening in phonon frequencies arises due to two factors. First, the C-B and B-B bonds are longer and are weaker compared to the C-C bonds, as pointed out earlier. Additionally, the C-C bonds around the rotating unit also get elongated due to the substantial strain introduced by B doping, and thus, get weakened. The rotation of the bond is easier in such a softer environment, which eventually reduces the SW activation barrier.

C. Reaction rate and characteristic time scale

At temperatures well below the melting point, the harmonic approximation to transition state theory (HTST) can be applied to study the reaction rate or characteristic time scale associated with the reaction. The reaction rate can be expressed in terms of energy and normal mode frequencies at the saddle point and initial state,\(^{35}\)

\[
k_{\text{HTST}} = \frac{\prod_{i}^{N} \nu^{I}_{i} \nu^{I}}{\prod_{i}^{N} \nu^{\text{TS}}_{i} \nu^{\text{TS}}_{i}} e^{-(E_{a}/k_{B}T)},
\]

where \(E_{a} = (E^{\text{TS}} - E^{I})\) is the activation energy with \(E^{I}\) (\(E^{\text{TS}}\)) being the energy corresponding to the initial (transition) state and \(\nu_{i}\) are the corresponding normal mode frequencies. Within the harmonic approximation, the entropic effect to the reaction rate is included in the prefactor involving phonon frequencies calculated at zero temperature. The first-order transition state is characterized by one imaginary phonon, which is excluded for the transition state. To calculate the prefactor, we have considered only the normal modes corresponding to the 14-atom pyracyclene ring around the rotating dimer. The characteristic time scale associated with a given reaction can be calculated from the knowledge of reaction rate \(k_{\text{HTST}}\) as \(\tau = 1/k_{\text{HTST}}\). Figure 7 shows the characteristic time required for a single \(I_{h} \rightarrow C_{2v}\) SW transition plotted as a function of temperature.
of temperature. The characteristic time scale, measured in seconds, differs by $10^{10} - 10^6$ due to subsequent B doping in the temperature range of 1000–2000 K. For example, at 1700 K, a single SW bond rotation event takes place in ~10 days for pristine C_{60}. In contrast, at the same temperature, the process is enormously accelerated and requires only about a second and a microsecond for C_{60}B and C_{60}B_2, respectively. The reverse transition ($C_{2v} \rightarrow I_h$, which is not shown in Fig. 7) is $\exp(\Delta E/k_B T)$ times faster than the forward transition. For example, the reverse transition is 5 orders of magnitude faster for C_{60} at 1700 K.

IV. CONCLUSIONS

The SW activation barrier in pristine fullerenes is very large. It has been reported earlier that this high barrier can be reduced by ~55% due to the presence of an extra carbon or hydrogen.\(^2\)\(^3\)\(^5\) The present calculation shows that the presence of the substitutional boron at the active sites can become more effective in the reduction of the SW activation barrier. We show that it can be reduced substantially by ~30% and 60% via single and double B doping, respectively. Calculated bond strength, charge density, and phonon spectrum indicate that the C-B bonds are softer compared to the C-C bonds. Thus, the presence of such weaker bonds around the rotating dimer is responsible for the observed reduction in the activation barrier. From a thermodynamic point of view, such a reduction in the barrier $\Delta E_c$ enormously reduces the time scale associated with the SW process. The reduction is on the order of $\exp(\Delta E_c/k_B T)$, which is $10^6$-fold ($10^{12}$-fold) at a temperature of 1700 K for single (double) B doping. SW defects are known to alter the chemical reactivity toward adsorbates,\(^14\)\(^-\)\(^17\) and thus, are expected to affect the proposed reversible H\(_2\) storage properties of B heterofullerenes.\(^35\)\(^,\)\(^36\) Although we have shown the reduction in the SW activation barrier for fullerene here, a similar reduction is expected for carbon nanotubes and graphene nanostructures due to B doping, which could catalyze fusion, and the welding process necessary for nanoelectronic device applications.

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