INTERMODULAR DESCRIPTION SHEET: UMAP Unit 764

TITLE: Of Mites and Models: A Temperature-Dependent

Model of a Mite Predator-Prey Interaction

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Mathematical modeling, differential equations

APPLICATION FIELD: Population biology

TARGET AUDIENCE: Students in differential equations or mathematical

modeling courses that cover phase-plane analysis.

ABSTRACT: We analyze the qualitative behavior of a model for a

mite predator-prey interaction. This model is based on a simple system of differential equations, and the model parameters are assigned values determined for a specific interaction between two species of mites. Several of these parameters are functions of temperature, and temperature is treated as a bifurcation parameter in the analysis of the model. It is shown that, depending on the temperature value, the model exhibits a stable fixed point, a stable limit cycle, or both (bistability). The model is used to illustrate population outbreaks.

Prefequisites: Familiarity with the qualitative analysis of systems of

differential equations (phase-plane analysis), and availability of an ODE solver with an adaptive step size (e.g.,

a Runge-Kutta-Fehlberg method).

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